

Could dark matter or neutrinos discriminate between the enantiomers of a chiral molecule?

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ABSTRACT

We examine the effect of cold dark matter on the discrimination between the two enantiomers of a chiral molecule. We estimate the energy difference between the two enantiomers due to the interaction between fermionic WIMPs (weak interacting massive particles) and molecular electrons on the basis that electrons have opposite helicities in opposite enantiomers. It is found that this energy difference is completely negligible. Dark matter could then be discarded as an inductor of chiroselection between enantiomers and then of biological homochirality. However, the effect of cosmological neutrinos, revisited with the currently accepted neutrino density, would reach, in the most favorable case, an upper bound of the same order of magnitude as the energy difference obtained from the well known electroweak electron-nucleus interaction in some molecules.

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1 Introduction

The origin of biological homochirality, that is, the almost exclusive one-handedness of chiral molecules in biological organisms, is a fundamental problem for which there is not yet a convincing solution. Several mechanisms have been proposed to explain chiroselection among the two possible enantiomers of a chiral molecule (see for example [1, 2, 3] and references therein). These mechanisms involve chance, β -radiolysis [4], circularly polarized light [5, 6, 7], magnetic fields [8, 9], and violation of parity in the weak interaction (see below).

The discovery of an excess of L-amino acids in meteorites [10, 11] has reinforced the idea of an extraterrestrial origin of biological homochirality [1, 12]. In this context, universal mechanisms of chiroselection such as parity violation in weak interactions would acquire special interest in spite their tiny effects, without of course underestimating other mechanisms.

The effect of electroweak interactions between electrons and nuclei mediated by the Z^0 , have been extensively studied and observed in atoms (see the review [13]), and only predicted in molecules, where an energy difference between the two enantiomers of chiral molecules has been estimated to be between 10^{-16} and 10^{-21} eV [14, 15, 16, 17, 18]. In the laboratory, no conclusive energy difference have been reported in experimental spectroscopic studies reaching an energy resolution of about 10^{-15} eV [19].

The above tiny energy difference would require a powerful mechanism of amplification in order to induce a real enantioselective effect. Otherwise the small energy difference would be masked by the natural broadening of the energy levels of the molecule, thermal fluctuations and environment interactions, which do not discriminate, in average, between L and D enantiomers. There is active research on amplification mechanisms in which a permanent although very small interaction acting always in the same enantioselective direction, and under appropriate conditions, could lead to an effective enantioselection. Some mechanisms are based on nonlinear autocatalytic processes of polymerization or crystallization along a large period of time [20, 21]. Another one involves a second-order phase transition below a certain critical temperature [22] that could work at low temperatures such as those of the interstellar space. However, theoretical or experimental conclusive results from the diverse mechanisms to amplify enantioselection based on electroweak energy difference, are not yet at hand (e.g., [23, 24]).

Another universal mechanism that could discriminate between the two enantiomers of a chiral molecule and that involves weak interaction is neutrino-electron axial-vector interaction mediated by charged electroweak bosons W^\pm . This process discriminates on the basis of an asymmetry between the number of neutrinos and antineutrinos, and that electrons of opposite (L,R) enantiomers have opposite helicity. Considering the cosmological relic sea of neutrinos, the estimated energy difference between the two enantiomers was found to be even lower than the value 10^{-21} eV mentioned above [25]. However, it could increase significantly under bigger neutrino fluxes, as in supernova remnants [26] assumed that big molecules could survive in the surroundings. Revisited assumptions about the number density of cosmological neutrinos in the relic sea lead to an increase of the mentioned energy difference, as we shall see in the next section.

Looking for other universal mechanisms acting also outside of the Earth, we analyze here the possible enantioselective effect of chiral dark matter on chiral molecules.

The existence of dark matter is inferred from astrophysical observations in light of studies of the dynamics of stars in the local disk environment, rotation curves for a large number of spiral galaxies, gravitational lensing by clusters of galaxies and some large scale studies of the Universe (for a recent review of experimental searches for dark matter see for example [27]). A vast variety of candidates have been proposed for dark matter content, from baryonic to non-baryonic matter. The non-baryonic candidates are basically postulated elementary particles beyond the Standard Model which have not been discovered yet, like axions, WIMPs (Weak Interacting Massive Particles) and other exotic candidates. The baryonic candidates are the Massive Compact Halo Objects (Macho) [28]. Another important difference is the hot versus cold dark matter. A dark matter candidate is called hot if it was moving at relativistic speeds at the time when galaxies could just start to form, and cold if it was moving non-relativistically at that time. The problem is that hot dark matter cannot reproduce correctly the observed structure of the Universe. Therefore we focus our attention on cold dark matter. The fact that dark matter interacts weakly with matter makes its detection very difficult [27]. However many experiments are currently in progress in order to reach this goal.

Here we estimate the energy difference between the two enantiomers of a chiral molecule, due to the weak type interaction between non-baryonic cold dark matter (specifically WIMPs) and molecular electrons with non zero helicity. Experimental results on dark matter are used. Given the resemblance

in the procedure with the energy difference induced by cosmological neutrinos, estimated in a previous work [25], we first recall this procedure at the time we improve the result we obtained in that work.

2 Energy difference between opposite enantiomers induced by cosmological neutrinos

Following a previous work [25], we consider neutrino-electron interactions mediated by the axial-vector Hamiltonian density

$$H = \frac{G_F}{\sqrt{2}} \bar{e} \gamma^\mu (g_V - g_A \gamma_5) e \bar{\nu} \gamma_\mu (1 - \gamma_5) \nu, \quad (1)$$

where G_F is Fermi's constant, $e(\nu)$ denotes the electron (neutrino) spinor field, $\bar{e}(\bar{\nu})$ is its adjoint spinor, γ^μ are the Dirac matrices (regarded as a four-vector), $\gamma^5 = i\gamma^0\gamma^1\gamma^2\gamma^3$, and $g_{V,A}$ are suitable coupling constants that parameterize the strength of the interactions. As it was discussed for example in [29], in the non-relativistic limit it is possible to make the following approximations for the dominant temporal components of the four-vectors appearing in the above Hamiltonian,

$$\begin{aligned} \bar{e} \gamma^\mu \gamma_5 e &\sim \vec{\sigma}_e \cdot \vec{v}_e, \\ \bar{\nu} \gamma_\mu \nu &\sim n_\nu - n_{\bar{\nu}} \quad (\text{Dirac neutrinos}), \\ \bar{\nu} \gamma_\mu \gamma_5 \nu &\sim n_{\nu_l} - n_{\nu_r} \quad (\text{Majorana neutrinos}), \end{aligned} \quad (2)$$

where the number density differences, $n_\nu - n_{\bar{\nu}}$ and $n_{\nu_l} - n_{\nu_r}$ refer to neutrino-antineutrino and left-right helicity eigenstates respectively. Obviously they are not zero only in the case where there is a net lepton number or helicity in the cosmic neutrinos background. We recall from [25] and [30] that for Dirac neutrinos the energy splitting obtained for the electron is

$$\Delta E \sim G_F |(n_\nu - n_{\bar{\nu}}) \langle \vec{\sigma}_e \cdot \vec{v}_e \rangle|, \quad (3)$$

where the expected value of the electron helicity $\langle \vec{\sigma}_e \cdot \vec{v}_e \rangle$ takes opposite signs for the two opposite enantiomers, as we can see from a simplified chiral molecule model [31]. In this model, a dominant axial symmetry around axis Z, with a left(right)-handed perturbative potential of period a, is assumed, so that the electronic molecular states can be described by superposition of

eigenstates of both angular momentum L_z and linear momentum P_z (eigenvalues $\hbar n(2\pi/a)$), i.e. $|M_L, n\rangle$, in the form

$$\Phi_L = c_0|0, 0\rangle + c_1|+1, -1\rangle + c_2|-1, +1\rangle, \quad (4)$$

$$\Phi_R = c_0|0, 0\rangle + c_1|+1, +1\rangle + c_2|-1, -1\rangle, \quad (5)$$

with $|c_1|^2 = |c_2|^2 \equiv C$. These L and R states have then opposite helicities:

$$\langle \Phi_L | L_z P_z | \Phi_L \rangle = -4C\pi/a = -\langle \Phi_R | L_z P_z | \Phi_R \rangle. \quad (6)$$

Notice that we are using all the time natural units where $\hbar = c = 1$. The spin of the electron can be taken into consideration by replacing L_z with $J_z = L_z + S_z$. In a realistic chiral molecule the electronic states would not be eigenstates of the helicity, but its mean value would have opposite sign for L and R enantiomers. The parameter $C < 1/2$ accounts for the degree of chirality.

We note that the velocity of the molecule carrier (interstellar grains, meteorites, the Earth...) does not contribute to the helicity of the electrons: If \vec{P}_T is the translational momentum of the carrier, the electronic wave function $\Phi_{L(R)}$ must include the factor $e^{i\vec{P}_T \cdot \vec{R}}$ (here \vec{R} is the position of the molecule), and the contribution of \vec{P}_T to the electron helicity is then

$$\begin{aligned} & \langle \Phi_{L(R)} e^{i\vec{P}_T \cdot \vec{R}} | \vec{L} \cdot \vec{P}_T | \Phi_{L(R)} e^{i\vec{P}_T \cdot \vec{R}} \rangle \\ &= \langle \Phi_{L(R)} | \vec{L} | \Phi_{L(R)} \rangle \cdot \vec{P}_T = 0, \end{aligned} \quad (7)$$

since $\langle \Phi_L | \vec{L} | \Phi_L \rangle = \langle \Phi_R | \vec{L} | \Phi_R \rangle = 0$ as can be seen from Eqs. (4,5). We also remark that the particle flux is assumed to be isotropic, thus, its interaction with the electrons of a chiral molecule is the same irrespective of the orientation of the molecule.

The energy difference that we obtained, assuming complete neutrino-antineutrino asymmetry, with number density of about 10^{-2}cm^{-3} , $C = 1/2$, $a \sim 1$ Angstrom and the electron helicity given by Eq. (6), was of the order of 10^{-26} eV [25].

However, it has been recently suggested [29, 32] that, in scenarios beyond the standard model, the neutrino-antineutrino density asymmetry $n_\nu - n_{\bar{\nu}}$ could be up to the order of $\sim 10 - 1050 \text{ cm}^{-3}$. Although the extreme upper bound density asymmetry seems to be excluded by considerations of primordial nucleosynthesis [33], we consider it to estimate an upper bound of the energy difference.

If we take the value $n_\nu - n_{\bar{\nu}} \sim 1000 \text{ cm}^{-3}$, we then obtain an upper bound for the energy difference between enantiomers of the order of 10^{-21} eV , per molecular electron with non zero helicity. Evidently this tiny energy needs massive amplification mechanisms as those mentioned at the beginning in order to induce an effective enantioselection.

3 Energy difference between opposite enantiomers induced by fermionic cold dark matter

In a similar way to the neutrino-electron interaction above considered, we are now to estimate the electron energy splitting induced by the axial-vector interaction between a fermionic dark matter candidate (typically a WIMP) and an electron. The relevant Hamiltonian density can be written as

$$H = \sum_i d_i \bar{\chi} \gamma_\mu (1 - \gamma_5) \chi \bar{\psi}_i \gamma^\mu \gamma_5 \psi_i, \quad (8)$$

where χ is the dark matter spinor which can be Dirac or Majorana. The index i runs through $i = e, u, d, s$, i.e., we are considering also the interaction between the dark matter particle and the u, d and s quarks. This will be important later in order to use the present experiments trying to measure the WIMP flux on Earth to set some bounds on the possible effect of dark matter on opposite enantiomers. Therefore d_e, d_u, d_d and d_s are the coupling of the χ field to the different matter fields $e = \psi_e, u = \psi_u, d = \psi_d$ and $s = \psi_s$.

As WIMPs are typical examples of cold dark matter and heavy by definition, we can invoke again the non-relativistic limit. Thus, as it was the case of neutrinos, for Dirac WIMPs the term $\bar{\chi} \gamma_\mu \chi$ dominates with the temporal component of this vector being proportional to $n_\chi - n_{\bar{\chi}}$. For the Majorana case only the axial vector $\bar{\chi} \gamma_\mu \gamma_5 \chi$ remains and its temporal component becomes proportional to $n_{\chi_l} - n_{\chi_r}$, as in Eq. (2).

The expression for the corresponding electron energy splitting is similar to that of Eq. (3),

$$\Delta E \sim d_e |\Delta n \langle \vec{\sigma}_e \cdot \vec{v}_e \rangle|, \quad (9)$$

where Δn is the appropriate number density difference corresponding to the Dirac or the Majorana case. In principle these differences depend on the unknown nature of the dark matter and its evolution along the universe history. In the following we will write these differences as $|\Delta n| = \alpha n$ where

n is the total WIMP number density. Clearly the parameter α is a measure of the degree of particle-antiparticle or left-right asymmetry present in the dark matter respectively. For example, in the case of Dirac dark matter, $\alpha = 1$ indicates that all WIMPs are particles with no antiparticles present and $\alpha = 0$ means a complete particle-antiparticle symmetry. As in the neutrino case, interactions between molecular electrons with non zero helicity and cold dark matter could lead to an energy difference between the two enantiomers of a chiral molecule whenever the parameter α is different from zero. To have an estimation of the energy difference, we consider the interaction between WIMPs and an electron of a chiral molecule. Let $\rho = nM_\chi$ be the energy density of those WIMPs, with M_χ being their mass and n their number density. The density of WIMPs trapped in the gravitational potential wall of the galaxy is expected to be of the order of $\rho \sim 0.3 \text{ GeV cm}^{-3}$. Then the energy splitting can be written as

$$\Delta E \sim d_e \alpha \frac{\rho}{M_\chi} |\langle \vec{\sigma}_e \cdot \vec{v}_e \rangle|. \quad (10)$$

In order to see how important this splitting could be, we need to know which values of the coupling constant d_e are acceptable. In principle there is no any available experimental information about d_e . However one reasonable assumption that could be done is that all the d_i couplings are at least of the same order of magnitude. In the absence of a theory of WIMPs this seems to be not so bad assumption since WIMPs does not interact strongly with matter. If this is the case, one can then use the present bounds on the elastic cross-section proton- χ to get some information about the size of the d_i couplings. In order to compute this cross section, one needs to relate the quark- χ couplings with the proton- χ coupling. This can be done by using the effective Hamiltonian (see [34] and references therein)

$$H = -a_p 2\sqrt{2} \bar{\chi} \gamma_\mu \gamma_5 \chi \bar{p} s^\mu p, \quad (11)$$

where p is the proton spinor and s^μ is its spin vector (here we are considering the Majorana case but the Dirac case can be treated in a similar way). The coupling a_p is defined as

$$a_p = \frac{1}{\sqrt{2}} \sum_{i=u,d,s} d_i \Delta q_i^{(p)}. \quad (12)$$

The constants $\Delta q_i^{(p)}$ (with $q_1 = u$, $q_2 = d$ and $q_3 = s$) are introduced through the proton matrix element

$$\langle p | \bar{\psi}_i \gamma^\mu \gamma_5 \psi_i | p \rangle = 2s^\mu \Delta q_i^{(p)}. \quad (13)$$

Experimentally we have $\Delta u^{(p)} \simeq 0.78$, $\Delta d^{(p)} \simeq -0.5$ and $\Delta s^{(p)} \simeq -0.16$. Then, by using standard methods, it is straightforward to compute the elastic proton- χ cross-section, which is given in the proton rest frame by

$$\frac{d\sigma}{dq^2} = \frac{\sigma_n}{4v_\chi\mu^2}, \quad (14)$$

where \vec{q} is the momentum transfer, v_χ is the χ velocity, μ is the proton- χ reduced mass and

$$\sigma_n = \frac{12a_p^2 m_p^2 M_\chi^2}{\pi(m_p + M_\chi)^2} \quad (15)$$

(m_p being the proton mass) is just the non-relativistic cross section for vanishing momentum transfer. Now days there are many experiments around the world trying to detect WIMPs directly (visit the webpage [35] for complete and upgraded report of their main results). Usually they set exclusion regions on the plane $\sigma_n - M_\chi$. From the recent XENON10 2007 [35] we learn for example that, for $M_\chi \simeq 100$ GeV, σ_n must be lesser than 10^{-43} cm² and, for $M_\chi \simeq 1000$ GeV, lesser than 10^{-42} cm². Assuming for simplicity all the quark couplings to be the same, i.e. $d_q \simeq d_u \simeq d_d \simeq d_s$, we have $a_p \simeq 0.0072d_q^2$. Then we get that for $M_\chi \simeq 100$ GeV, $d_q^2 < 10^{-14}$ GeV⁻⁴ and for $M_\chi \simeq 1000$ GeV, $d_q^2 < 10^{-13}$ GeV⁻⁴. As discussed above we now assume $d_e \sim d_q$. Then it is possible to set a bound on the energy splitting which turn to be very tiny even in best case corresponding to $M_\chi \simeq 100$ GeV. We obtain in this case, with an electron velocity about 10^{-2} , $\Delta E \leq \alpha 10^{-44}$ eV.

4 Conclusion

We have analyzed the effect of cold dark matter on the discrimination between the two enantiomers of a chiral molecule whose external electrons have opposite helicities in the respective opposite enantiomers. The estimated energy difference between the two enantiomers, due to WIMP-electron interaction, is found to be extremely small, several orders of magnitude lower than that induced by electron-nuclei weak interaction. Hence, dark matter would be discarded as inductor of chiroselection between enantiomers and then of biological homochirality. By contrast, the enantioselective effect of the cosmological relic sea of neutrinos acquires relevance with the current assumptions about the number density of cosmological neutrinos. In this case we obtain an energy difference between 10^{-23} and 10^{-21} eV for the two opposite enantiomers per molecular electron with non zero helicity. The upper bound of the energy difference, although could be excluded by reasons

previously mentioned, reaches the same order of magnitude as the energy difference induced by the well known electron-nucleus electroweak interaction in some molecules.

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